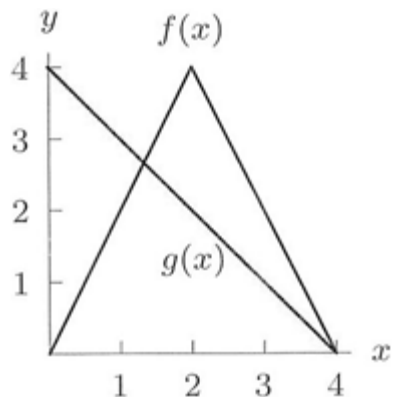


Sheet # 341 Chain Rule and Graphs

The functions $f(x)$ and $g(x)$ are defined in the below Figure. [Figure 3.17, CSV 3.4, p.131, Questions 53–56.]

Make tables with x as rows and function values as columns. Some quantities do not exist.

Chain rule formula for the derivative of a composite function: $[f(g(x))]' = f'(g(x)) \cdot g'(x)$.



1. Find:

$f(0), f(1), f(2), f(3), f(4)$.

$g(0), g(1), g(2), g(3), g(4)$.

$f'(0), f'(1), f'(2), f'(3), f'(4)$.

$g'(0), g'(1), g'(2), g'(3), g'(4)$.

2. Find:

$g(f(0)), g(f(1)), g(f(2)), g(f(3)), g(f(4))$.

3. Find:

$g(g(0)), g(g(1)), g(g(2)), g(g(3)), g(g(4))$.

4. Let $m(x) = f(2x)$.

Find **in two ways**, using **graph** and chain rule **formula**:

$m'(0), m'(0.5), m'(1), m'(1.5), m'(2), m'(3), m'(4)$.

5. Let $k(x) = f(x/2)$.

Find:

$k'(0), k'(1), k'(2), k'(3), k'(4), k'(6), k'(8)$.

6. Let $r(x) = f(4x)$.

Find using chain rule **formula**:

$r'(0), r'(0.25), r'(0.5), r'(1), r'(2), r'(4)$.

7. Let $u(x) = g(f(x))$. [Same as question 54.]

Find **in two ways**, using **graph** and chain rule **formula**:

$u'(1), u'(2), u'(3)$.

8. Let $w(x) = g(g(x))$. [Same as question 56.]

Find:

$w'(1), w'(2), w'(3)$.